Critical-Path and Priority based Algorithms for Scheduling Workflows with Parameter Sweep Tasks on Global Grids

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Abstract

Parameter-sweep has been widely adopted in large numbers of scientific applications. Parameter-sweep features need to be incorporated into Grid workflows so as to increase the scale and scope of such applications. New scheduling mechanisms and algorithms are required to provide optimized policy for resource allocation and task arrangement in such a case. This paper addresses scheduling sequential parameter-sweep tasks in a fine-grained manner. The optimization is produced by pipelining the subtasks and dispatching each of them onto well-selected resources. Two types of scheduling algorithms are discussed and customized to adapt the characteristics of parameter-sweep, as well as their effectiveness has been compared under multifarious scenarios.

1. Introduction

The emergence of Grid computing has largely expanded the scale of scientific applications [1]. Among the programming models designed for Grid computing, combining dependent tasks into workflow systems [2] has received attention in recent past.

Related research efforts on workflow management have focused on how to define and manipulate the workflow model, compose distributed software components and data/documents together, as well as how to reduce the global execution time or to fully utilize available resources to achieve stated objectives [3]. However, within Grid scale scientific applications, the presence of repeated tasks have motivated introduction for mechanism to group and manage such tasks. Let us consider the following scenario:

Suppose a data-analysis application consists of three steps. Firstly, the experiments will gather data from a remote sensor array. Each sensor in the array will be required to collect data under the configuration of specific parameters. Then, the result data will be staged to several data process centers. These centers will filter the raw data to structured data, according to the locally deployed knowledge databases on associated computational resources. The remote filtering operation needs to be divided into smaller tasks and carried out in parallel – staging it as one workload can cause overloading of both the selected computational resource and the database. At last, the filtered data will be gathered to a scientific computing visualization cluster for post-processing (e.g. visualization).

Now the scientist is going to establish a workflow in order to automate the experiment. From the designer's point of view, the simplest definition is to assign each step as a single task, hence a (pipeline) task-graph representing the workflow would be:

$$Collecting(A) -> Filtering(B) -> Visualization(C)$$

The task A and B are collections of one or more subtasks representing repeated execution of a job. In this case, operations within data collection and filtering tasks are performed over different sets of data. Such individual tasks are called *parameter-sweep* tasks [4].

A characteristic of parameter-sweep task is that there is no inter-communication between its subtasks. However, it introduces a new challenge as it requires optimization of the execution of such parameter-sweep tasks within workflow. In a workflow application scenario shown in Figure 1, it is clear that a subtask in task B need not wait for all the results from task A to be generated before it's starting. A subtask in B can be launched once a certain portion of the results from A is available. In this manner, the makespan of the application execution could be reduced substantially.

In this paper, we focus on the mechanisms and algorithms that implement the *fine-grained* optimization mentioned above. We discuss both the static and dynamic scheduling methodologies, while extending two
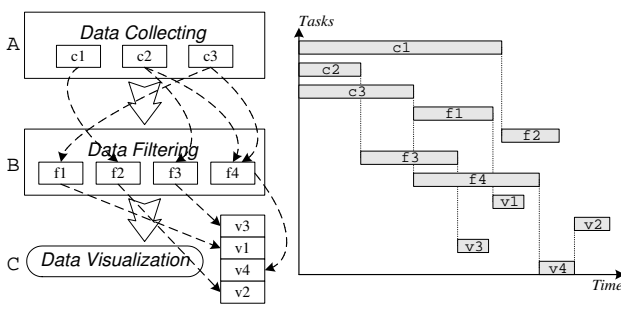
Figure 1. Optimizing the example parameter-sweep workflow.

well-known algorithms and customizing them to achieve the best effectiveness under task graphs with parameter-sweep tasks. The extended algorithms, called xDCP and pM-S, are derived from the existing Dynamic Critical Path (DCP)[5] and Master-Slave (M-S)[6] algorithms respectively. The xDCP extends the original DCP in order to support the scheduling among resources with different capabilities. The pM-S tries to give higher priority to the sub-task-graph which is estimated to complete earlier. Finally, we analyze the proposed algorithms by comparing their behaviors under different experimental scenarios.

The rest of the paper is organized as follows. A formal definition of the optimization problem is presented in section 2. Section 3 will discuss about the possible optimization toward parameter-sweep tasks in workflow. Experiments and data are given in section 4. Section 5 discusses the related work. Section 6 presents the conclusion with the direction for future work.

2. Optimization Problem

2.1. Problem statement

This sub-section gives the formal description of the optimization problem.

Let $\Gamma = \bigcup_{i=1}^{K} T_i$ be the task space, including K sequential parameter-sweep tasks and $N(T_i)$ refers to the number of subtasks in T_i. Hence, for each T_i, there are $T_i = \{t_{ij} | j = 1..N(T_i)\}$. The length of subtask t_{ij} is referred by $l(t_{ij})$, while $L(T_i) = \{l(t_{ij}) | j = 1..N(T_i)\}$. For each i where $1 < i \leq K$, we define the task dependency of T_i: $D(T_i) = \{d(t_{ij}) | j = 1..N(T_i)\}$, where $d(t_{ij}) = \{k | t_{(i-1)k} \prec t_{ij}\}$. The symbol $\prec$ is a newly defined binary relation that $\prec (t_a, t_b)$ (also marked as $t_a \prec t_b$) means task t_b must be put into execution strictly after the accomplishment of task t_a. Based on the task dependency, we can define a subtask's parents and children. The func-

tion $Parents(t) : \Gamma \to \bigcup_{i=1}^{K} T_i^*$ (where T_i^* is T_i's closure) refers to the set of all the subtasks that subtask t directly depends on, formally:

$$Parents(t_{ij}) = \begin{cases} \phi, & if\ i = 1 \\ \{t' | t' \in T_{i-1}, t' \prec t_{ij}\}, & if\ i \neq 1. \end{cases}$$

Also we have $Children(t) : \Gamma \to \bigcup_{i=1}^{K} T_i^*$ that

$$Children(t_{ij}) = \begin{cases} \phi, & if\ i = K \\ \{t' | t' \in T_{i+1}, t_{ij} \prec t'\}, & if\ i \neq K. \end{cases}$$

The resources are defined corresponding to the tasks. Assume $\Omega = \bigcup_{i=1}^{K} R_i$ to be the resource space, in which $R_i = \{r_{ij} | j = 1..N(R_i)\}$ refers to the array of resources specially for running all the subtasks in T_i, where $N(R_i)$ refers to the number of individual resources in the resource array. Note the resource here refers to *virtual* resource instead of physical resources like clusters or supercomputers with one or more nodes. For physical resources, we could have $\mho = \{\Re_j | j = 1..M\}$ representing the resource space available. Each virtual resource presents a share of a physical resource that is available for executing a particular parameter-sweep task. A physical resource could be shared by multiple virtual resources, providing different services to different tasks in the workflow. In the following sections, the term "resources" is used to represent virtual resources.

We define the throughput of a single resource r_{ij} to be marked as $p(r_{ij})$, so that for a subtask t_{ix} and one of its corresponding resources r_{iy}, the time for r_{iy} to finish t_{ix} will be

$$\omega(t_{ix}, r_{iy}) = \frac{l(t_{ix})}{p(r_{iy})}$$

Let $P(R_i) = \{p(r_{ij}) | j = 1..N(R_i)\}$.

The optimization lies on the problem of resource queueing. In most cases, the length of resource array will be much less than the number of subtasks in a parameter-sweep task. That means, some subtasks are required to be executed on the same resource. We assume all the resources follow the rule of exclusive. That is, resources are allocated using space-shared scheduling policy. All resources are non-preemptive and exclusive in execution (e.g., using queueing system such as PBS for managing resources).

Having defined all the related concepts, the problem statement is defined as follows:

Problem: Given $\{(T_i, R_i, D(T_i), L(T_i), P(R_i)) | i = 1..K\}$. Select the mapping $f(t) : \Gamma \to \Omega$ to minimize $Time(\Gamma, \Omega)$ under the rule-of-exclusive, where $Time(\Gamma, \Omega)$ refers to the total execution time.

3. Mechanisms and Algorithms

There exist two types of scheduling mechanisms, namely, static scheduling and dynamic scheduling. In this

section, we discuss the scheduling and optimization under both the two scenarios.

3.1. Static scheduling

The simplest solution of a static schedule is to allocate all the subtasks in a shuffle way, namely assign task t_{ij} to $r_{i(j\%N(R_i))}$. However, due to the irregularity of both the subtasks and the resources, shuffle scheduling might lead to the inefficient result as less powerful resources may be assigned heavy subtasks leading to imbalance in completion time of various tasks.

Numerous works [8][9] have addressed the topic of static scheduling of task graphs. However, task graphs/workflows with parameter-sweep tasks have some special features compared to normal task graphs:

1. Subtasks and resources are grouped in layers (parameter-sweep tasks). A subtask t_{ij} is allowed to be scheduled to R_i.

2. There is no dependency between subtasks in the same layer.

3. Every subtask depends (if there exist dependency) on only the subtasks in its parent layer, as it is specified in section 2.

Based on these criteria, we modified the DCP algorithm, so that it could be adopted well for scheduling workflows with parameter-sweep tasks. For convenience, we denote the proposed algorithm by *xDCP* (e*x*tended *DCP*).

The DCP algorithm based on the principle of continuously shortening the longest path (also called *critical path (CP)*) in the task graph, by scheduling tasks in the current CP to an earlier start time. The algorithm was designed for scheduling all tasks to the same set of homogeneous resources. However, the workflow scenario we defined in section 2 is about scheduling different sets of tasks onto different sets of irregular/heterogeneous resources.

To tackle with the above conflict, basically we import the following extensions into the original DCP algorithm:

1. The initialization of DCP algorithm is to queue all tasks sequentially in one resource, while leaving other resources empty. In xDCP, we first initialize the tasks in a shuffle way. Experiments show that this adjustment can improve the effectiveness of DCP by 30% in workflows with parameter-sweep tasks.

2. The DCP algorithm uses the term *absolute earliest/latest start time (AEST/ALST)*, which means the possible earliest/latest start time of a subtask on its current resource. In particular, if a certain task can have a smaller AEST on resource A than resource B, then assignment to A will be regarded as a better schedule for this task. However, in a scenario with heterogenous resources, the executing time of the same task on each resource is different. Therefore we have to use another term *absolute earliest/latest finish time (AEFT/ALFT)* (means the possible earliest/latest finish time of a subtasks on its current resource) to evaluate the schedule.

3. The DCP algorithm ends if all the tasks have been scheduled once. However, we found that under workflow with parameter-sweep tasks it will deliver an extra 10%-20% effectiveness if we further run DCP again on the scheduled result.

4. DCP considers the communication overhead incurred in implementing the task dependency. However, there is no inter-process communication between the subtasks of a parameter-sweep task. Therefore we simply remove the terms in DCP that related to the communication cost. Also, we removed the deadlock checking in DCP algorithm according to the nature of parameter sweep tasks.

Now we provide a formal description of the xDCP algorithm. First, we will discuss the definition of the previous and next subtask of a certain subtask in its resource queue:

In a given resource mapping $f(\sigma) : \Gamma \to \Omega$, for any subtask t, we have its previous and next subtasks mapped in the same resource queue. Formally:

$$Prev(t) = \begin{cases} \psi, & if \ \forall t' \in \Gamma, \nexists f(t') = f(t) \wedge t' \preceq t \\ \\ t', & if \ f(t') = f(t) \wedge t' \preceq t \\ & \wedge (\forall t'' \in \Gamma, \nexists t' \preceq t'' \preceq t) \end{cases}$$

$$Next(t) = \begin{cases} \psi, & if \ \forall t' \in \Gamma, \nexists f(t') = f(t) \wedge t \preceq t' \\ \\ t', & if \ f(t') = f(t) \wedge t \preceq t' \\ & \wedge (\forall t'' \in \Gamma, \nexists t \preceq t'' \preceq t') \end{cases}$$

Then comes the definition of *AEFT, DCPL (dynamic critical path length)* and *ALFT (absolute latest finish time)*:

A subtask can be started only after all its parent subtasks are finished, and all the previous tasks in the same resource queue are also finished. The earliest finish time can be calculated by adding the execution time on the current resource onto the earliest start time. In a given resource mapping $f(\sigma) : \Gamma \to \Omega$, the absolute earliest finish time of any subtask t, denoted by $AEFT(t)$ is recursively defined as follows:

$$AEFT(t) =$$

$$\begin{cases} 0, & if \ t = \psi \vee (Parents(t) = \phi \wedge Prev(t) = \psi) \\ \\ \max\{\max_{\forall \tau \in Parents(t)}\{AEFT(\tau) + \omega(t, f(t))\}, \\ AEFT(Prev(t)) + \omega(t, f(t))\}, & otherwise \end{cases}$$

The dynamic critical path length of the task graph is another form for defining the term $Time(C, R)$ in section 2 by using the AEFT:

$$DCPL(f, \Gamma, \Omega) = \max_{\tau \in \Gamma}\{AEFT(\tau)\}$$

Having the DCPL, we can define the latest finish time of a subtask. The DCPL is the summation of the execution time of all the subtasks on the critical path of the task graph. Therefore, if we want to finish the whole execution by the time of DCPL, all the subtasks on the critical path should be finished at exactly their AEFT. The absolute latest finish time of subtask t should be no later than the latest start time of all its children subtasks and its next subtask in the same resource queue. We define it as:

$$ALFT(t) =$$

$$
\begin{cases}
DCPL(f, \Gamma, \Omega), \\
\qquad if \ \ t = \psi \vee (Childrens(t) = \phi \wedge Next(t) = \psi) \\
\\
\max\{\max_{\forall \tau \in Children(t)}\{ALFT(\tau) - \omega(\tau, f(\tau))\}, \\
ALFT(Next(t)) - \omega(Next(t), f(Next(t)))\}, \\
\qquad\qquad\qquad\qquad\qquad\qquad\qquad otherwise
\end{cases}
$$

The xDCP algorithm is listed below:

1. Shuffle all the subtasks in Γ onto the resources in Ω. Let $DCPL = 0$;

2. $\forall t \in \Gamma$, set t to be unallocated;

3. $\forall t \in \Gamma$, compute $AEFT(t)$ and $ALFT(t)$;

4. Let t be the subtask t_{ij} selected from Γ which, orderly, follow the three criterions below:

    (a) Minimize the value of $ALFT(t_{ij}) - AEFT(t_{ij})$;

    (b) Minimize the value of i;

    (c) Minimize the value of $AEFT(t_{ij})$;

5. $\forall r \in \Omega$, select r and the slot in r's queue that, assuming t is allocated onto this slot, orderly satisfying:

    (a) $ALFT(t) - AEFT(Prev(t)) \geq \omega(t, f(t))$;

    (b) Minimize the value of $AEFT(t)$;

    If there exists such a resource and slot, move t onto the selected slot of r, or else not move anything;

6. Set t_{ij} allocated. If $\exists t \in \Gamma$ unallocated, goto 3);

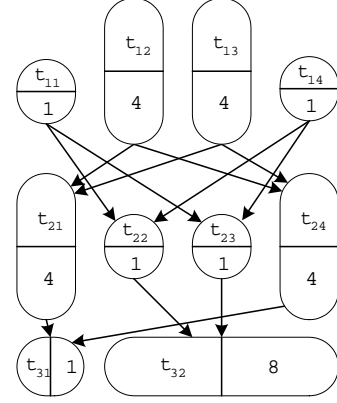7. If $DCLP(f, \Gamma, \Omega)/DCLP * 100\% < 95\%$, goto 2); or else the algorithm ends.

Figure 2. An example task graph.

3.2. Dynamic scheduling

A most-commonly used dynamic scheduling mechanism is the *Master-Slave (M-S) model*. The M-S model is proven to be quite efficient under most scenarios. For the workflow applications with parameter-sweep tasks, we employ K masters corresponding to K parameter-sweep tasks. For each master there are two queues instead of only one queue in the original M-S model. Initially, all the subtasks are stored in the *Unscheduled* queue. There is another queue called the *Ready* queue. Only subtasks in the Ready queue can be directly dispatched to slave nodes. At the start of scheduling, all the subtasks t with $Parents(t) = \phi$ can be put into the Ready queue, and then some of them (on the head of the Ready queue) will be dispatched. On the accomplishment of subtask t, the master will check all the subtasks in the $Children(t)$. We put all the subtasks in the set

$$UtoR(t) = \begin{array}{l} \{t' | t' \in Children(t) \wedge (\forall t'' \in Parents(t'), \\ \nexists Queue(t'') = Unscheduled)\} \end{array}$$

into their Ready queue respectively. There are two threads for a master. One of them is responsible for dispatching subtasks in the Ready queue onto slaves, while the other is to stage subtasks from the Unscheduled queue to the Ready queue.

However, the M-S model will still fail to achieve effectiveness under some cases. Consider the task graph shown in Figure 2 (with the length $l(t)$ of each subtask indicated). Suppose in $R_1 = \{r_{11}\}, R_2 = \{r_{21}, r_{22}\}, R_3 = \{r_{31}\}$, where $\forall r \in \Omega, p(r) = 1$. From Figure 4 we can see that there should be possibility of a parallelization between the two subtasks in T_1 with the length of 4 and the longest subtask in T_3, namely t_{32}. However, by following the M-S model, the master have to execute the subtasks in T_1 sequentially (because there is only one resource in R_1), which holds t_{32} from being dispatched earlier (due to its indirect dependency to t_{14}).
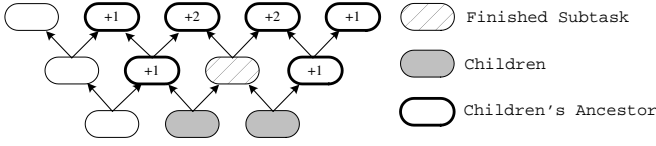
Figure 3. An example of priority calculation.

A priority based mechanism is proposed in this paper to deal with the above problem. In this mechanism, we assume that it would be effective to bring forward the subtasks whose children's ancestors (refer to Figure 3) have been partially finished or already being put into execution. Base on this assumption, we define the priority of each subtask according to how much its children's ancestors have been finished.

Before we list the new algorithm, a term $Ancestors(t)$ should be defined, which refers to all the subtasks that t directly or indirectly depends on:

$$Ancestors(t) =$$

$$\begin{cases} \phi, & if \ Parents(t) = \phi \\ (\bigcup_{t' \in Parents(t)} Ancestors(t')) \cup Parents(t), & otherwise \end{cases}$$

Also the term of the priority and two types of queues: Let $Pri(t)$ denotes the priority of subtask t. Let the Ready queue to be denoted by $Q_R(T_i, \preccurlyeq)$, the Unscheduled queue is denoted by $Q_U(T_i, \preccurlyeq)$, where $\preccurlyeq (x, y)$ is a binary relation that $\forall x, y = 1..N(T_i)$,

$$Pri(t_{ix}) * N(T_i) + x < Pri(t_{iy}) * N(T_i) + y \Leftrightarrow t_{ix} \preccurlyeq t_{iy}$$

means lower the value of $Pri(t)$, higher the priority. For both the queues, the *head* subtask is defined as $Head(Q(T, \preccurlyeq)) = t$, where $t \in T \land (\forall t' \in T, \nexists t' \preccurlyeq t)$. The head refers to the subtask with the highest priority, and will be scheduled first.

The priority of subtasks will be updated on the event of any subtask being finished. As it is shown in Figure 3, once a subtask has been finished, the master first collects all its children into a set. Then it parses all the elements of the set. For each children subtask, all its ancestors will receive an unit-increment on their priority (namely $Pri(t) = Pri(t) - 1$). After the priority adjustment, the master will retrieve a certain number of tasks, according to the allocation status, from the head of the Ready queue and then dispatch them into execution.

The new algorithm, denoted by *pM-S*, is listed below:

1. $\forall t \in \Gamma, Pri(t) = 0. \ \forall T_i \in \Gamma, Q_R(T_i, \preccurlyeq) = \{t | t \in T_i \land Parents(t) = \phi\}, Q_U(T_i, \preccurlyeq) = \{t | t \in T_i \land Parents(t) \neq \phi\}$.
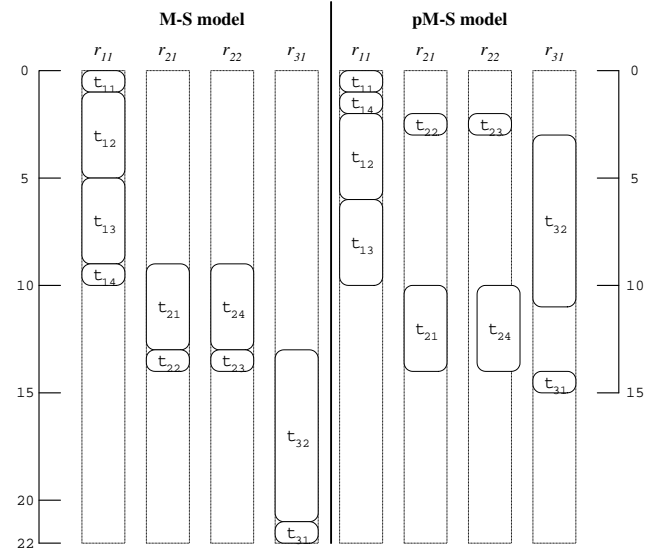
2. For $i = 1$ to K, do

Figure 4. Comparison of the finish time of subtasks in Figure 2 under M-S model and pM-S model.

   (a) For $j = 1$ to $N(R_i)$, if $Q_R(T_i, \preccurlyeq) = \phi$ then break the current for-j-loop; if r_{ij} is not empty, continue the current for-j-loop; or else dispatch the subtask $Head(Q_R(T_i, \preccurlyeq))$ to the resource r_{ij}.

3. If all subtasks in Γ have been scheduled, then algorithm ends;

4. Wait for the event of any subtask t's execution being finished;

5. For each subtask $\tau \in \bigcup_{\forall t' \in Children(t)} Ancestors(t')$, $Pri(\tau) = Pri(\tau) - 1$;

6. Stage subtasks in $UtoR(t)$ to their Ready queues respectively, goto 2).

The right part of Figure 4 shows the schedule result produced by pM-S algorithm. It only costs 15 time units while the M-S schedule costs 22.

4. Performance evaluation

In this section, we present the comparative evaluation of static and dynamic algorithms (shuffle, xDCP, M-S and pM-S).

4.1. Metrics and important factors

Since we use randomly generated task graphs in the experiments with factors discussed in sub-section 4.2, a sta-

tistical analysis will be adopted in this paper by calculating and presenting the mean value for a large number of scenarios. Basically we have two metrics for this simulation.

Average Scheduling Effectiveness (ASE): The ASE refers to a ratio (in the format of percentage) between the to-be-measured algorithm and the shuffle algorithm in terms of the simulated total execution time of the whole application after the schedule. Lower the ASE value, higher the effectiveness resulted.

Average Beat-down Time (BDT): A *beat-down* of an algorithm means the algorithm has produced the best scheduling result out of all the to-be-measured algorithms under certain task graph. For each experiment we try 30 randomly generated task graphs. The algorithm which wins the lowest ASE in the competition is supposed to have the highest BDT.

There are also some important factors which can affect the schedule effectiveness:

Range of subtask size (RSS) and of resource throughput (RRT): The range of subtask size can be presented as the ratio between the size of the longest subtasks and the shortest one in the same parameter-sweep task. Let the RSS value for all the parameter sweep tasks to be the same. RRT is similar to RRS, substituting the subtask size to resource throughput. Let the RRT value for all the parameter sweep tasks to be the same. We set the RSS and RRT as the boundary of generating random task size and resource throughput. Then we multiply the random value by a base value (each parameter-sweep task has its own base value $\bar{l}$ for task and $\bar{p}$ resource respectively), to get the final value of individual subtask size and resource throughput.

Ratio #Subtask/#Resource (RSR): This ratio will also be calculated inside the parameter-sweep task. As the value of RSR increases, the size of resource queue will be also increased.

Number of parameter-sweep tasks (#PST): As the workflow has more and more parameter-sweep tasks (namely the task graph owns more and more layers), the dependency structure will get more complicated; a shuffle algorithm will leave more gaps in its output schedule, hence the space for optimization will be enlarged.

Average number of the dependencies per subtask (ADPS: This value can be presented as:

$$ADPS = \frac{\sum_{i=2..K} N(D(T_i))}{\sum_{i=2..K} N(T_i)}$$

The index i starts from 2 because T_1 has no dependency at all, thus it will not be counted in either the numerator or the denominator.

Factor	#PST	RSS	RRT	RSR	ADPS	$\bar{l}$	$\bar{p}$
#PST	3-12	5	5	5	2	20	10
RSS	5	1-10	5	5	2	20	10
RRT	5	5	1-10	5	2	20	10
RSR	5	5	5	1-10	2	20	10
ADPS	5	5	5	5	1.0-5.5	20	10

Table 1. The configuration of all the measured factors.

4.2. Measurement for randomly generated task graphs

We consider about the randomly generated task graphs. For fairness, the total number of subtasks is fixed at 512, although the number of subtasks in each parameter-sweep tasks might be randomly generated.

For the random task graphs, we observe how the ASE (Figure 5) and BDT (Figure 6) value varies with the factors listed above, for the algorithm xDCP, M-S and pM-S. When we change the value of a factor, the other factors will remain constant at a default value. The configuration of all the factors are shown in Table 1. From the Figure 5, we can conclude:

1. The increment of #PST slightly raises the effectiveness of algorithm M-S and pM-S, while drops the effectiveness of algorithm xDCP.

2. The increment of RSS almost has no effect on the effectiveness of algorithm M-S and pM-S, but slightly raises the effectiveness of algorithm xDCP.

3. The increment of RRT raises the effectiveness of all the three algorithms in a large extent.

4. The increment of RSR dramatically raises the effectiveness of all the three algorithms.

5. The increment of ADPS drops the effectiveness of all the three algorithms, but it affects to the xDCP more than the other two algorithms.

By comparing algorithms in Figure 6, we find that in most measured cases, the pM-S will be the best choice for scheduling. However, under the cases of the #PST and RSR decreases, or RRT increases to a certain value, or the ADPS equals to 1, the xDCP may become more effective. That is, the M-S algorithm is always not the best choice.

5. Related Work

In [10], a dynamic, adaptive algorithm is proposed for adjusting the scheduling queue in Grid based task farming applications. The algorithm can keep the queue size to fit
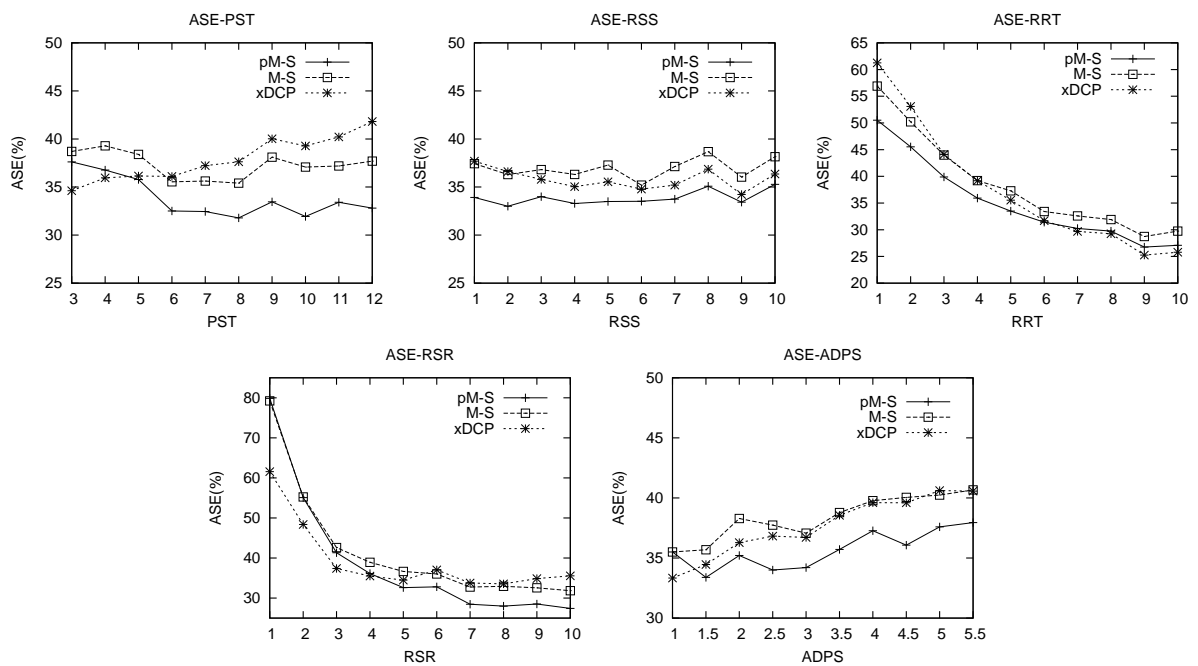
Figure 5. Average Scheduling Effectiveness (ASE) varies with PST, RSS, RRT, RSR and ADPS.
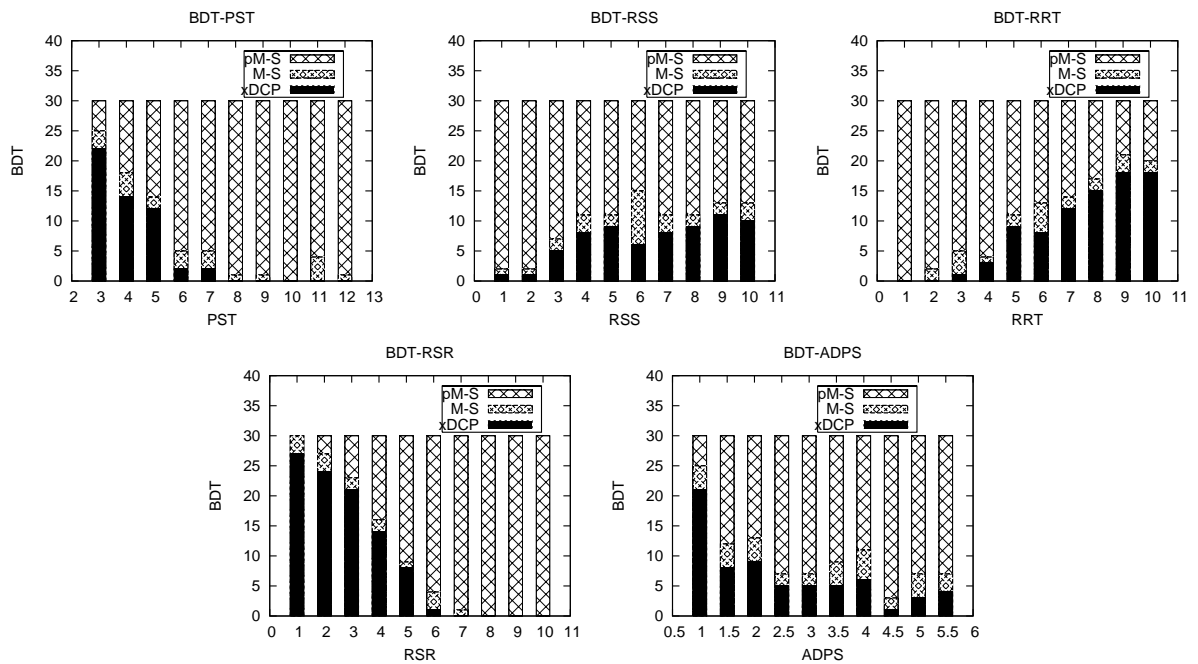

Figure 6. Average Beat-down Time (BDT) varies with PST, RSS, RRT, RSR and ADPS.

the computational capability of current environment. This is a type of implementation of the M-S algorithm, and can certainly be also adopted in our pM-S algorithm.

A pipeline model has been proposed in [11] for task farming in Grid. However, the mechanism it discusses is actually conventional Master-Slave based, with no priority involved. According to the experiment results in section 4, there is still a gap between the effectiveness of M-S and our pM-S algorithm. Also, [11] has not mentioned about optimizing the scenario of multiple parameter-sweep tasks linked together.

The work in [12] focuses on how many slave resources needed in a task farming application where the number of subtasks is given, to achieve the certain effectiveness. Several factors are used to construct the model. Similarly, in this paper we use more elaborate factors like RSS, RRT and RSR to establish our metrics model, in order to give more precise evaluation on the algorithm's effectiveness.

In [13], a model of Resource Efficiency (RE) is given to help evaluating the effectiveness of task farming scheduling algorithms. In our work, we use the average ratio (ASE) between the total waiting time of the to-be-measured algorithm and the shuffle algorithm. We adopt ASE value instead of RE because even under the same configuration of factors, the topology of task graph might still result a remarkable influence on the performance of algorithms, hence gives the distribution of waiting time a large deviation and makes the average value meaningless. By using ASE, the influence of task graph topology could be shielded by the performance of the shuffle algorithm, hence will do little interference on the evaluation result.

6. Conclusion and future work

In this paper, we have presented two algorithms that address the problem of optimal scheduling of workflow applications with parameter-sweep tasks. The experiment results shown in section 4 have indicated the effectiveness of the proposed algorithms. Also, we compared the algorithms under different configuration and sample task graphs, which shows our effort on comprehensively examining the useability of each algorithm.

In the paper, we assume every parameter-sweep task consume its resource array exclusively. This constraint can be removed by letting each task of workflow utilize multiple resources from Grid resource space, which makes the scheduling optimization more complicated, because the algorithm need to consider not only the transverse subtasks in the same parameter-sweep task, but also vertical subtasks sharing the same set of resources.

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